The retina dose-area histogram:
a metric for quantitatively comparing rival eye plaque treatment options

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Abstract

Purpose: Episcleral plaques have a history of over a half century in the delivery of radiation therapy to intraocular tumors such as choroidal melanoma. Although the tumor control rate is high, vision-impairing complications subsequent to treatment remain an issue. Notable, late complications are radiation retinopathy and maculopathy. The obvious way to reduce the risk of radiation damage to the retina is to conform the prescribed isodose surface to the tumor base and to reduce the dose delivered to the surrounding healthy retina, especially the macula. Using a fusion of fundus photography, ultrasound and CT images, tumor size, shape and location within the eye can be accurately simulated as part of the radiation planning process. In this work an adaptation of the dose-volume histogram (DVH), the retina dose-area histogram (RDAH) is introduced as a metric to help compare rival plaque designs and conformal treatment planning options with the goal of reducing radiation retinopathy.

Material and methods: The RDAH is calculated by transforming a digitized fundus-photo collage of the tumor into a rasterized polar map of the retinal surface known as a retinal diagram (RD). The perimeter of the tumor base is digitized on the RD and its area computed. Area and radiation dose are calculated for every pixel in the RD.

Results: The areal resolution of the RDAH is a function of the pixel resolution of the raster image used to display the RD and the number of polygon edges used to digitize the perimeter of the tumor base. A practical demonstration is presented.

Conclusions: The RDAH provides a quantitative metric by which episcleral plaque treatment plan options may be evaluated and compared in order to confirm adequate dosimetric coverage of the tumor and margin, and to help minimize dose to the macula and retina.

Key words: eye plaque, episcleral plaque, brachytherapy, retina, dose-area histogram.
retinal edema appears to reduce the severity of RM. These complications are progressive and may have a delayed onset of months to years after radiation treatment. The severity is dependent on the dose rate, the total dose of radiation and the amount of retina irradiated.

The obvious way to reduce vision-impairing complications is, to the extent practical, to conform the prescribed isodose surface to the target volume and reduce the dose delivered to those photosensitive portions of the retina that fall outside of the target volume, with particular attention to the macula. The dose prescription target volume for intraocular tumors, illustrated in Fig. 1, is typically defined by the apex of the tumor and a small retinal margin (e.g. 2 mm) surrounding the tumor base. This margin accounts for microscopic extension of the tumor and uncertainties associated with plaque placement. This margin is analogous to the planning target volume (PTV) concept. Therefore, the objective of conformal plaque therapy is to enclose the tumor apex and base + margin within the prescribed isodose surface while sparing as much of the surrounding tissue as possible.

Fortunately, the gold shell of the plaque absorbs virtually all primary radiation emanating from the radionuclide seeds that is initially directed away from the eye, and because the dome portion of the tumor is surrounded by radiobiologically inert vitreous humor, it is not critical for the isodose surface to closely conform to the shape of the dome in order to achieve the radiobiological goals of conformal therapy. It is primarily the dose delivered to the target volume and to the retina that are of radiobiological concern, and therefore it is sufficient that the prescribed isodose surface covers, and preferably conforms to, the shape of the base (+ margin) of the tumor.

Image-based treatment simulation software for ophthalmic plaques that could model the conformal treatment of intraocular tumors was initially developed and adopted for clinical use at the University of Southern California (USC) in the early 1990s and has been in continuous development ever since [10-16]. This software fuses fundus photography, ultrasound, and either computed tomography (CT) or magnetic resonance (MR) images to build interactive three-dimensional (3D) virtual models of each patient’s ocular anatomy, the plaques and the radiation sources. The software was licensed for commercial distribution in 1994 under the title Plaque Simulator™ (Eckert & Ziegler BEBIG GmbH, Robert-Rössle-Str.10, D-13129 Berlin, Germany). Gold plaques featuring collimating slots for each radiation source, introduced in the late 1990s [15] demonstrated that highly conformal treatment of ocular tumors was possible.

A fundamental requirement of all conformal external beam radiotherapy treatments (e.g. radiosurgery) is precise patient and beam positioning. A conformal isodose plan with a steep dose gradient outside the target volume is of little clinical value if it cannot be reliably delivered. An analogous situation applies to conformal plaque treatment. If the plaque is not positioned on the eye at the location and orientation intended by the plan, then portions of the tumor may receive less dose than intended, and the healthy retina could receive more dose than intended.

Historically, the information regarding tumor size, shape and location within the eye that was often provided for plaque treatment planning purposes consisted of approximations and hand-drawn sketches. Occasionally, at the time of surgery, a plaque might be found to be too small, perhaps due to intervening tumor growth, requiring the plaque to be reconfigured while the patient remained under sedation or risk inadequate coverage of the tumor base. The position on the eye at which the plaque would be affixed was not determined until the time of surgery during which a bright light was used to transilluminate the eye and cast a shadow of the tumor base onto the underlying translucent sclera. This shadow was traced with a marker pen and the plaque positioned to cover the tumor base. In aviation parlance, this approach is analogous to “flying by the seat of one’s pants” compared to using a predetermined flight plan and instruments. Under these conditions, conformal treatment and calculation of dose to the retina was not practical.

Using image-based 3D treatment simulation, the tumor location can be accurately determined and plaque position can be planned in advance of surgery. To facilitate accurate positioning at the planned position, the simulation software provides targeting support in the form of suture eyelet coordinates on the sclera in a format familiar to the ophthalmic surgeon. Coordinates are expressed as a meridian clock hour (see Fig. 3) and a chord distance from the limbus (see Fig. 1) for each suture eyelet of the plaque [12,16]. In practice, the meridian clock hours can be estimated to within a few minutes by the surgeon, and the chord distance on the meridian...
precisely measured using an adjustable Castroviejo caliper. The 2 mm PTV margin surrounding the tumor base takes into account the uncertainty in locating the meridian. Nearly two decades of experience using this coordinate system at USC has demonstrated that it is simple and reliable. Providing suture coordinates also frees the plaque shell from having to physically conform to the shape of the tumor base, it is sufficient that the radiation sources mounted within the shell provide the conformal isodose coverage when the shell is positioned as planned. Freeing the shape of the shell from the physical shape of the tumor enables the suture eyelets to be relocated to more convenient anterior locations where suturing is easier and more accurate.

Although both the hardware, software and a targeting system now exist for planning and delivering conformal treatment of intraocular tumors, until now a means of quantitatively comparing rival treatment plan options has been lacking. In conventional radiation therapy treatment planning, the dose-volume histogram [17] (DVH) has proven itself a useful tool for comparing rival treatment plans. In this work an adaptation of the DVH concept, the retina dose-area histogram (RDAH) is introduced as a quantitative tool for the comparison of rival plaque designs and treatment plan options with the ultimate goal of reducing radiation retinopathy.

Material and methods

The Plaque Simulator™ (PS) software [10-16] was modified to version 5.7 to support the simultaneous calculation and display of RDAHs for up to 4 rival plaque configurations. In this version of the software histograms are calculated for the photosensitive region of the retina between the posterior pole and the ora serrata, the macula, the tumor base, the base plus retinal margin and for photosensitive retina outside the base and margin. In the PS software, the sclera posterior to the equator is modeled as a 1 mm thick hemispherical shell. Sclera anterior to the equator is modeled as a 1 mm thick oblate spheroidal shell which intersects the dome-shaped cornea. The 1 mm scleral shell thickness is an assumption carried forward from the model of the eye that was recommended by the COMS, but it appears to be adequate for treatment planning purposes.

Referring again to Fig. 1, the photosensitive portion of the retina is modeled as a lining covering most of the interior surface of the sclera. The ora serrata delineates the transition from the simple non-photosensitive area of the retina near the ciliary body to the complex, multi-layered photosensitive region. The location of the ora serrata in the computer model is specified by a user adjustable ora-angle. Describing the photosensitive extent of the retina by a single angle enables the model to adapt to eyes of different spherical and oblate radii of curvature with minimal user intervention. The PS default for this angle is 123.3 degrees.

The determination of the size, shape and location of the tumor base on the retina begins with a digitized fundus-photo collage of the retina which must include the macula, the optic disc, and as much of the tumor as can be photographed [12]. The center of the optic disk and the posterior pole near the macula are readily identifiable landmarks on the collage. After these two locations are marked on the collage, as illustrated in Fig. 2A, the 3D coordinate of every pixel in the collage can be calculated relative to those landmarks once the 3D coordinates of those landmarks are determined. Returning the fundus collage to 3D space also requires that the radius of curvature of the retina be known, and, in what direction the camera was looking when photographing each of the smaller pictures that make up the collage. In Fig. 2A, the approximate centers of most of the photos that make up the collage are marked to indicate where the central ray of the camera was pointing when photographing that region of the retina.

The PS coordinates of the posterior pole, the center of the optic disk and the radius of curvature of the retina initially default to the COMS recommended standard model of the eye. If available, a transverse axial CT image which bisects the eye through the poles and the optic nerve...
the posterior pole at the macula, and which shows the optic nerve entering the eye can be used to customize the PS model to match the spherical or oblate curvature of the actual patient eye as illustrated in Fig. 2B. In general, the slice spacing is too great, and the resolution of CT and MRI is too low to reliably determine tumor size and shape within the eye. However, by finding a common pair of landmarks in both the fundus photos and CT images, the pixels of the fundus collage can be transformed to 3D space and fused with the CT or MRI study to reveal the tumor location for a specific patient. Occasionally, the taller tumors are visible in CT and MRI and this has proven useful for confirming the fundus collage 3D transform. CT and MRI are also very useful companions to ultrasound for estimating the size, shape and location of anterior tumors which cannot be photographed.

The tumor location is determined by projecting the digitized fundus collage onto a two dimensional (2D) map of the retinal surface and then manually outlining the tumor base [12]. Using the earth as an analogy, the spherical surface of the eye is most commonly represented using the cylindrical Mercator projection in which size and shape distortion is minimal at the equator and maximum at the poles. In the eye, however, the region of greatest visual interest surrounds the posterior pole, not the equator. The retinal diagram (RD) is a polar map of the retinal surface from the posterior pole to the limbus. On a polar map, size and shape distortion is minimal at the polar center of the diagram and increases with the radial distance from the pole. For the RD illustrated in Fig. 3, observe that on the diagram the distance representing a unit distance (e.g. 1 mm) in 3D space is radially constant, but stretches circumferentially with radial distance from the polar center of the diagram. For example, the RD circle representing the great circle of latitude at the equator of the eye is drawn with a smaller diameter, and the circumferential distance between 1 mm tic marks on the equatorial circle of the RD is smaller than for the circle on the RD which represents the circle of latitude at the ora serrata which lies in the anterior hemisphere of the eye. The circle of latitude at the ora is, of course, three dimensionally much smaller than the circle at the equator.

There is an exact transformation between the retinal surface in 3D space and the RD, and most objects of interest near the retina, such as the tumor apex, the extraocular muscle insertion locations, the plaque perimeter and the radiation sources can be projected onto the RD as illustrated in Fig. 3. Note that all 3D objects mapped onto the retinal diagram, including the fundus photoglage, must be circumferentially stretched according to their latitude as was illustrated for the circle of latitude at the ora.

After the perimeter of the tumor base has been outlined on the RD, the points defining the perimeter polygon can be transformed back into 3D coordinates on the retina, and a PTV-like margin added by expanding the perimeter polygon on the spherical and/or oblate shaped surface of the retina as determined from the CT images. A 2 mm margin is illustrated as a thin brown line surrounding the nominally elliptical tumor base in Fig. 3. The 3D model of the tumor is completed by using ultrasound imaging to determine the shape and height of the tumor dome resulting in an interactive 3D model that includes the ocular anatomy, the tumor, the plaque, the suture coordinates and the calculated radiation dosimetry as illustrated in Fig. 4.

Once the 3D model and its RD projection have been created, rival treatment planning options, such as the choice of radionuclide, and the number and location of radiation sources, may be quantitatively compared using a retina dose-area histogram. The dose-area histogram for the surface of the retina is calculated by first plotting a raster image analogous to the RD seen in Fig. 3, except that the image contains only the tumor and margin against a plain white background. The area on the spherical surface of the retina represented by a pixel on the rasterized RD varies with its latitude, so the area of each pixel in the RD image is calculated as a function of latitude, and then the coordinates of the center of that pixel are transformed from RD space to 3D space and the dose delivered at that point is calculated. The areas are binned as a function of dose for the object they represent on the RD, and plotted in a manner analogous to the ubiquitous dose-volume histogram.

The objects for which dose-area will be calculated are: (1) the entire photosensitive surface of the retina represented by RD pixels that fall within the ora circle, (2) pixels that fall within the tumor perimeter anywhere on the diagram, (3) pixels that fall outside of the tumor perimeter and within...
the ora circle, (4) pixels that fall within the margin surrounding the tumor base, (5) pixels that fall outside of the margin and within the ora circle and (6) pixels that fall within the macular region which is approximated as a 5 mm diameter disc surrounding the posterior pole. In practice, this is easily accomplished by filling the tumor base and margin perimeter polygons on the raster image with different colors which encode what objects those pixels belong to and simply sorting according to the color of each pixel when binning the object areas. The raster image method is robust in that it works for polygons of arbitrary size and shape. The spatial resolution of the histogram will increase, as will the calculation time, as a function of the number of pixels that comprise the RD on the raster image.

**Results**

The surface area $A$ of a spherical dome, or equivalently, a spherical bowl is

$$A = 2\pi r_c h$$

where $r_c$ is the radius of curvature of the sphere and $h$ is the height of the dome, or equivalently, the depth of the bowl as illustrated in Fig. 5. The height $h$ can be calculated from the chord diameter $d$ of the dome at its base and the curvature of the sphere as

$$h = r_c (1 - \cos(asin((d/2)/r_c)))$$

For a 24 mm equatorial diameter spherical eye, and assuming that the retina is inset 1 mm from the external surface of the eye, the radius of curvature of the retina $r_c = 11$ mm. The retinal surface area covered by a tumor with a circularly shaped base of chord diameter $d = 10$ mm is 83.08 mm².

The spatial resolution of the histogram, and hence, the visual smoothness of the plotted dose-area curves, increases with the number of pixels that comprise the RD on the raster image. However, increasing the number of pixels proportionally increases the calculation time.

Table 1 summarizes results obtained when varying the RD image resolution for the same eye and tumor description for which the analytical solution was calculated above. The tumor is assumed to have a circular base of chord diameter 10 mm approximated by a polygon consisting of 36 edges and a retinal spherical radius of curvature of 11 mm. Because the tumor perimeter is defined by a polygon, we expect the calculated area to be slightly less than the 83.08 mm² derived from the analytical solution above. The third column in Table 1 is the number of colored pixels that fell within the margin surrounding the tumor base.

![Fig. 4. 3D fusion of CT imaging, fundus photography, ultrasound measurements, plaque, suture eyelets, surgical coordinates and radiation dosimetry](image)

![Fig. 5. Diagram illustrating the terms used in the analytical solution of the spherical surface of a tumor with a circular base of chord diameter (d), spherical radius of curvature (r_c) and dome height (h)](image)

<table>
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<tr>
<th>RD diameter (pixels)</th>
<th>Polygon edges</th>
<th>Tumor base (pixels)</th>
<th>Calculated area (mm²)</th>
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Table 1. The leftmost column is the diameter, measured in pixels, of the RD in the rasterized image that is used to calculate the RDAH. The retina was modeled as being spherical with a radius of curvature of 11 mm. The second column is the number of polygon edges that were used to approximate the circular base of a 10 mm chord diameter tumor. The third column is the number of pixels that filled the polygon on the RD image. Note that although pixels on the RD image are all identical squares, the area that each pixel represents on the spherical surface varies with its radial distance from the pole of the RD. The rightmost column is the area on the spherical surface of the retina occupied by the tumor base. It is calculated by numerically integrating the areas of the pixels that filled the tumor polygon. The analytical solution for the area of this tumor on the spherical surface is 83.08 mm².
pixels that filled the polygon on the RD image. Recall that although pixels on the rasterized RD image are all identical squares, the area of spherical surface that each pixel represents varies with its radial distance, or latitude, from the pole of the RD. The rightmost column is the area on the spherical surface of the retina occupied by the tumor base. It is calculated by numerically integrating the areas of the pixels that filled the tumor polygon.

In Table 2 the number of polygon edges used to draw the tumor on the RD image is varied from 24 to 180. As expected, the numerical integration approaches the analytical solution as the perimeter of the polygon approaches a circle.

### Table 2

The description of Table 2 is the same as Table 1 except that here the number of polygon edges used to draw the tumor on the RD image is varied from 24 to 180. The analytical solution for the area of this tumor on the spherical surface is 83.08 mm². As expected, the numerical integration approaches the analytical solution as the perimeter of the polygon approaches a circle.

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<th>Tumor base (pixels)</th>
<th>Calculated area (mm²)</th>
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<tr>
<td>1024</td>
<td>180</td>
<td>19 030</td>
<td>83.0</td>
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Discussion

The threshold dose for retinal damage is generally considered to be about 30-35 Gy. Emami et al. [22] report 5%/5yr normal tissue tolerance for retina to be 45 Gy and 50%/5yr tolerance to be 65 Gy. Animal studies have shown damage to rods with 20 Gy and to cones with 100 Gy. Although damage to photoreceptors has been reported, it is the inner retinal layers and retinal vascular endothelial cells that are the most affected, causing vessel closure and ischemic (capillary dropout) retinopathy which, in turn, leads to additional forms of damage including neovascularization which can induce secondary glaucoma, retinal detachment, and vitreous hemorrhage [9]. When the macula and fovea are
Fig. 6. Five rival treatment options for a 3.4 mm tall, elliptically shaped tumor. A) COMS 14 mm plaque fully loaded with I-125 seeds. B) COMS 14 mm plaque with its carrier rotated to enable a partial loading of the carrier with I-125 seeds to dosimetrically conform to the shape of the tumor and its 2 mm retinal margin. C) Ru-106 model CCA beta-ray plaque. D) Similar to B) except that the I-125 seed closest to the macula has been removed and replaced by two adjacent seeds of half weighting. E) COMS 14 mm shell modified with a gold insert in place of the silicone seed carrier and semi-conformally loaded as in D) except with Pd-103 seeds. In all cases the plaques were automatically centered under the tumor and a dose of 85 Gy was prescribed to the apex of the tumor. From left to right, the columns illustrate the radionuclide loading of the plaque, isodose lines on the retina, and isodose lines on a meridian plane bisecting the eye through the tumor apex. Isodose lines are plotted for the range 40 to 300 Gy. The yellow 300 Gy isodose line is unlabeled.
Fig. 7. A) Retina dose-area histograms for the rival plans presented in Figs. 6A, 6B and 6C. The dashed lines are the COMS 14 mm plaque (Fig. 6A) fully loaded with I-125 seeds. The heavy solid lines are the COMS 14 mm plaque (Fig. 6B) conformally loaded with I-125 seeds. The intermittent dash-dot lines are the model CCA Ru-106 beta-ray plaque (Fig. 6C). The blue curves are the areal dose to the photosensitive portion of the retina that lies outside the margin that surrounds the tumor base. The orange curves represent the macular region. These are the regions where the radiation dose should be minimized as best possible. B) Retina dose-area histograms for the plans presented in Figs. 6B, 6D and 6E. The heavy solid lines represent the COMS plaque conformally loaded with I-125 seeds (Fig. 6B). The dashed lines represent the semi-conformal COMS plaque (Fig. 6D) with the I-125 seed closest to the macula relocated to the adjacent carrier positions as two half-strength seeds. The intermittent dash-dot lines represent the gold-insert-modified COMS plaque (Fig. 6E) semi-conformally loaded with Pd-103 seeds.
involved, radiation maculopathy typically results in blindness [8,9].

In Figs. 7A and B, the orange and blue colored RDAH curves are of particular interest, because they plot relative area as a function of dose to the macular region and to the photosensitive portion of the retina that lies outside the PTV-like margin that surrounds the tumor base. These are the regions where one would like to reduce radiation dose with particular attention to areas which exceed normal tissue tolerance (e.g. 45 Gy).

With regard to the retina outside the margin (blue lines), the COMS plaque conformally loaded with I-125 sources (Fig. 6B), plotted as the thickest blue line, irradiates the least area to doses above 40 Gy. The Ru beta-ray plaque irradiates the least area for doses below about 25 Gy. With regard to the macula (orange curves), which happens to lie just above the posterior lip of the plaques in this particular example, the conformally loaded plaque (Fig. 6B), plotted as the thick orange lines, performs poorly. It delivers a much higher maximum dose to the macula and consistently irradiates a greater area of the macula as a function of dose. This occurs because it uses the fewest number of seeds of the highest individual activity and one of those seeds happens to be positioned very close to the macula.

In Figs. 6D and 7B observe that by removing the I-125 seed closest to the macula and redistributing its original area as a function of dose to the macular region and to the curves are of particular interest, because they plot relative 

ness [8,9].

The retina dose-area histogram provides a quantitative metric by which rival episcleral plaque treatment plan options may be quickly compared with regard to tumor and margin coverage, and possibly reducing the severity of subsequent radiation retinopathy and maculopathy. As with the dose-volume histogram, spatial location is lost in this method of analysis, so it must always be used as a companion to 2D and 3D isodose maps when making decisions regarding patient treatments.

Conclusions

The retina dose-area histogram provides a quantitative metric by which rival episcleral plaque treatment plan options may be quickly compared with regard to tumor and margin coverage, and possibly reducing the severity of subsequent radiation retinopathy and maculopathy. As with the dose-volume histogram, spatial location is lost in this method of analysis, so it must always be used as a companion to 2D and 3D isodose maps when making decisions regarding patient treatments.

References